

### Appendix B-1a Properties of Sections

$A$  = area, in.<sup>2</sup>

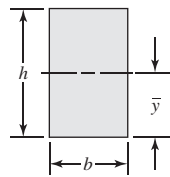
$I$  = moment of inertia, in.<sup>4</sup>

$J$  = polar moment of inertia, in.<sup>4</sup>

$Z$  = section modulus, in.<sup>3</sup>

$\rho$  = radius of gyration, in.

$\bar{y}$  = centroidal distance, in.



Rectangle

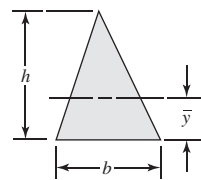
$$A = bh$$

$$I = \frac{bh^3}{12}$$

$$Z = \frac{bh^2}{6}$$

$$\rho = 0.289h$$

$$\bar{y} = \frac{h}{2}$$



General triangle

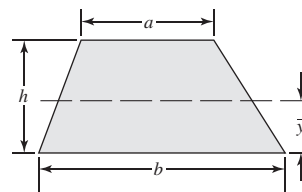
$$A = \frac{bh}{2}$$

$$I = \frac{bh^3}{36}$$

$$Z = \frac{bh^2}{24}$$

$$\rho = 0.236h$$

$$\bar{y} = \frac{h}{3}$$



General trapezoid

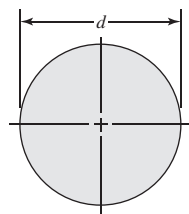
$$A = \frac{h}{2}(a + b)$$

$$I = \frac{h^3(a^2 + 4ab + b^2)}{36(a + b)}$$

$$Z = \frac{h^2(a^2 + 4ab + b^2)}{12(a + 2b)}$$

$$\rho = \frac{h}{6} \sqrt{2 + \frac{4ab}{(a + b)^2}}$$

$$\bar{y} = \frac{h(2a + b)}{3(a + b)}$$



Circle

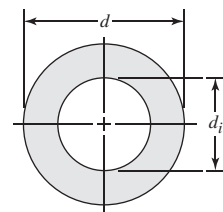
$$A = \frac{\pi d^2}{4}$$

$$I = \frac{\pi d^4}{64}$$

$$Z = \frac{\pi d^3}{32}$$

$$J = \frac{\pi d^4}{32}$$

$$\rho = \frac{d}{4}$$



Hollow circle

$$A = \frac{\pi}{4}(d^2 - d_i^2)$$

$$I = \frac{\pi}{64}(d^4 - d_i^4)$$

$$Z = \frac{\pi}{32d}(d^4 - d_i^4)$$

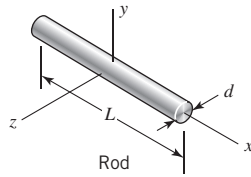
$$J = \frac{\pi}{32}(d^4 - d_i^4)$$

$$\rho = \sqrt{\frac{d^2 + d_i^2}{16}}$$

## Appendix B-2 Mass and Mass Moments of Inertia of Homogeneous Solids

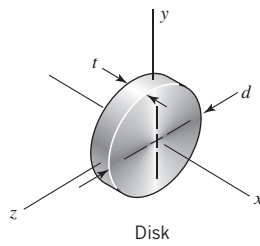
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$\rho$  = mass density



$$m = \frac{\pi d^2 L \rho}{4}$$

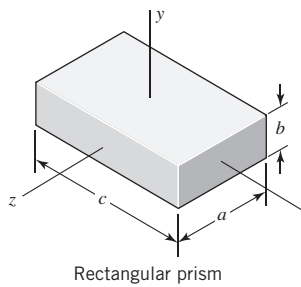
$$I_y = I_z = \frac{mL^2}{12}$$



$$m = \frac{\pi d^2 t \rho}{4}$$

$$I_x = \frac{md^2}{8}$$

$$I_y = I_z = \frac{md^2}{16}$$

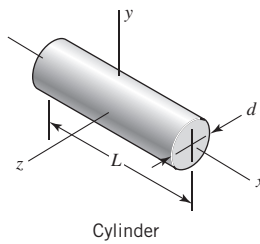


$$m = abc\rho$$

$$I_x = \frac{m}{12}(a^2 + b^2)$$

$$I_y = \frac{m}{12}(a^2 + c^2)$$

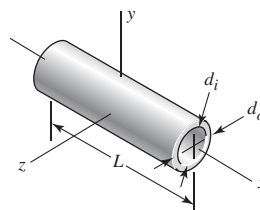
$$I_z = \frac{m}{12}(b^2 + c^2)$$



$$m = \frac{\pi d^2 L \rho}{4}$$

$$I_x = \frac{md^2}{8}$$

$$I_y = I_z = \frac{m}{48}(3d^2 + 4L^2)$$



$$m = \frac{\pi L \rho}{4}(d_o^2 - d_i^2)$$

$$I_x = \frac{m}{8}(d_o^2 + d_i^2)$$

$$I_y = I_z = \frac{m}{48}(3d_o^2 + 3d_i^2 + 4L^2)$$


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